GEOMETRY Dr. Paul L. Bailey Homework 0217 Wednesday, February 17, 2021

This homework is due Friday, February 19, 2021.

**Definition 1.** A polygon is *convex* if any line segment connecting two points on the polygon is contained inside the polygon. This is equivalent to the condition that all of its interior angles are less than  $180^{\circ}$ .

**Problem 1.** Show that every convex quadrilateral is divided by its diagonals into proportional triangles.

**Problem 2.** Let  $\triangle ABC$  be an isosceles triangle, with AB = AC. Let D be a point on  $\overline{AC}$  such that  $\overline{BD}$  bisects  $\angle ABC$  and  $\triangle BCD \sim \triangle ABC$ .

- (a) Carefully draw this.
- (b) Find  $m \angle ABC$  and  $m \angle BAC$ .
- (c) Show that  $\triangle DAB$  is isosceles.
- (d) Challenge: Find  $\frac{AB}{BC}$ .